

SOLVING EQUATIONS: PART 2

RECALL

In an **EQUATION**

...there is an equal sign

To **SOLVE** an Equation

...isolate the variable

We can follow the steps below to solve equations

C	Clear fractions by multiplying all terms by a common denominator.
E	Expand using the distributive law to eliminate brackets
I	Isolate the variable on one side of the equation using opposite operations
D	Divide by the numerical coefficient attached to the variable

i) $\frac{2x+10}{3} = 20$

$$\begin{aligned} & \cancel{3}(2x+10) = \cancel{3}(60) \\ & 2x + 10 = 60 \\ & 2x = 60 - 10 \\ & 2x = 50 \\ & \cancel{2} \quad \cancel{2} \\ & x = 25 \end{aligned}$$

ii) $6x + 5 = 4x - 7$

$$\begin{aligned} & 6x - 4x = -7 - 5 \\ & 2x = -12 \\ & \cancel{2} \quad \cancel{2} \\ & x = -6 \end{aligned}$$

ii) $\frac{x+3}{8} + \frac{x+1}{3} = 3$

Common denominator = 24

$$\begin{aligned} & \cancel{8}(x+3) + \cancel{3}(x+1) = 3 \times 24 \\ & 3(x+3) + 8(x+1) = 72 \\ & 3x + 9 + 8x + 8 = 72 \\ & 3x + 8x = 72 - 9 - 8 \\ & 11x = \frac{55}{11} \\ & \cancel{11} \quad \cancel{11} \\ & x = 5 \end{aligned}$$

iv) $3(x-1) + 1 = 5(x-2)$

$$\begin{aligned} & 3x - 3 + 1 = 5x - 10 \\ & 3x - 5x = -10 + 3 - 1 \\ & -2x = -8 \\ & \cancel{-2} \quad \cancel{-2} \\ & x = 4 \end{aligned}$$

EXAMPLES: Solve each of the following equations.

$$1. \ x - 4 = 12$$

$$x = 12 + 4$$

$$\boxed{x = 16}$$

$$2. \ 5x + 3 = 4x - 12$$

$$5x - 4x = -12 - 3$$

$$1x = -15$$

$$\boxed{x = -15}$$

$$3. \ 2x - 5 = 11$$

$$2x = 11 + 5$$

$$\frac{2x}{2} = \frac{16}{2}$$

$$\boxed{x = 8}$$

$$4. \ 3x - 11 = 5x + 3$$

$$3x - 5x = 3 + 11$$

$$\frac{-2x}{-2} = \frac{14}{-2}$$

$$\boxed{x = -7}$$

$$5. \ 8x + 13 - 3x = -26 + 2x$$

$$8x - 3x - 2x = -26 - 13$$

$$\frac{3x}{3} = \frac{-39}{3}$$

$$\boxed{x = -13}$$

$$6. \ 4(2x - 3) + 6 = (7 - 6x) + 5$$

$$8x - 12 + 6 = 7 - 6x + 5$$

$$8x + 6x = 7 + 5 + 12 - 6$$

$$\frac{14x}{14} = \frac{18}{14}$$

$$\boxed{x = \frac{9}{7} \text{ OR } 1.29}$$

$$7. \ \frac{r+5}{3} + 5 = -r$$

$$r + 5 + 15 = -3r$$

$$20 = -3r - r$$

$$\frac{20}{-4} = \frac{-4r}{-4}$$

$$\boxed{-5 = r}$$

$$8. \ 0.2v = 0.6v + 1.7$$

$$0.2v - 0.6v = 1.7$$

$$\frac{-0.4v}{-0.4} = \frac{1.7}{-0.4}$$

$$\boxed{v = -4.25}$$

$$9. \ 4(3g - 5) = -2(4g + 3g)$$

$$12g - 20 = -92 - 6g$$

$$12g + 6g = -92 + 20$$

$$\frac{18g}{18} = \frac{-72}{18}$$

$$\boxed{g = -4}$$